

# The semidirect product in a variety of right $\Omega$ -loops

E. Inyangala

University of Cape Town  
*Edward.Inyangala@uct.ac.za*

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Let  $\mathbf{C}$  be a fixed variety of universal algebras which has among its operations a binary  $+$ , a binary  $-$ , and a nullary  $0$  satisfying the identities  $x + 0 = x$ ,  $0 + x = x$ ,  $(x - y) + y = x$  and  $(x + y) - y = x$ . In this talk we construct the semidirect product (see [2]) in  $\mathbf{C}$  as the set-theoretical (cartesian) product equipped with the  $\Omega$ -algebra structure. This construction helps to develop the theory of crossed modules in  $\mathbf{C}$  independently of the definition given in [3].

## References

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- [3] G. Janelidze, *Internal crossed modules*, Georgian Math. J. 10 (2003), no. 1, 99-114.