Consider the eight puzzle depicted in the figure below. This is a familiar game with eight tiles arranged in a 3-by-3 configuration with one open square. Tiles can be moved up, down, left or right into the open square, creating a new open square in the space that is vacated. The problem is to find a sequence of moves that convert the initial scrambled configuration of tiles into a goal configuration in which the tiles are arranged in numerical order. The brute force method would be to use trees to obtain all possible configurations.

Write a C++ program which finds the solution by expanding the tree.