

TWK2A

Separable DEs

Problems

1. Solve $xy' = 4y$.
2. Solve $e^x yy' = e^{-y} + e^{-2x-y}$.
3. Solve $\frac{dP}{dt} = P - P^2$.
4. Show that an implicit solution of $2x \sin^2 y dx - (x^2 + 10) \cos y dy = 0$ is given by $\ln(x^2 + 10) + \csc y = c$. Find any singular solutions.
5. Find a function whose square plus the square of its derivative is 1.
6. Solve $dy - (y - 1)^2 dx = 0$.
7. Solve $\frac{dy}{x} = \left(\frac{2y+3}{4x+5}\right)^2$.
8. Solve $\frac{dQ}{dt} = k(Q - 70)$.
9. Solve $\frac{dy}{dt} + 2y = 1$ subject to $y(0) = \frac{5}{2}$.
10. Solve $y dy = x(1 + x^2)^{-1/2}(1 + y^2)^{1/2} dx$.
11. Solve $x^2 y' = y - xy$ with $y(-1) = -1$.
12. Solve $\frac{dN}{dt} + N = Nte^{t+2}$.
13. Solve $y' = \frac{xy+2y-x-2}{xy-3y+x-3}$.
14. Solve $(e^x + e^{-x})y' = y^2$.
15. Find a solution of $xy' = y^2 - y$ that passes through **(a)** $(0, 1)$, **(b)** $(0, 0)$, **(c)** $(\frac{1}{2}, \frac{1}{2})$, **(d)** $(2, \frac{1}{4})$.